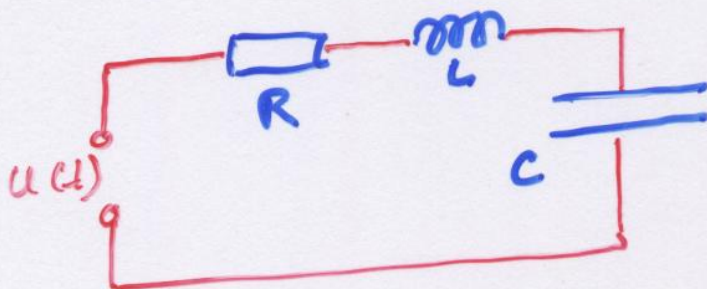


$$R_L = \omega L \quad \text{Impedanz}$$

6. Spule + ohmscher Widerstand

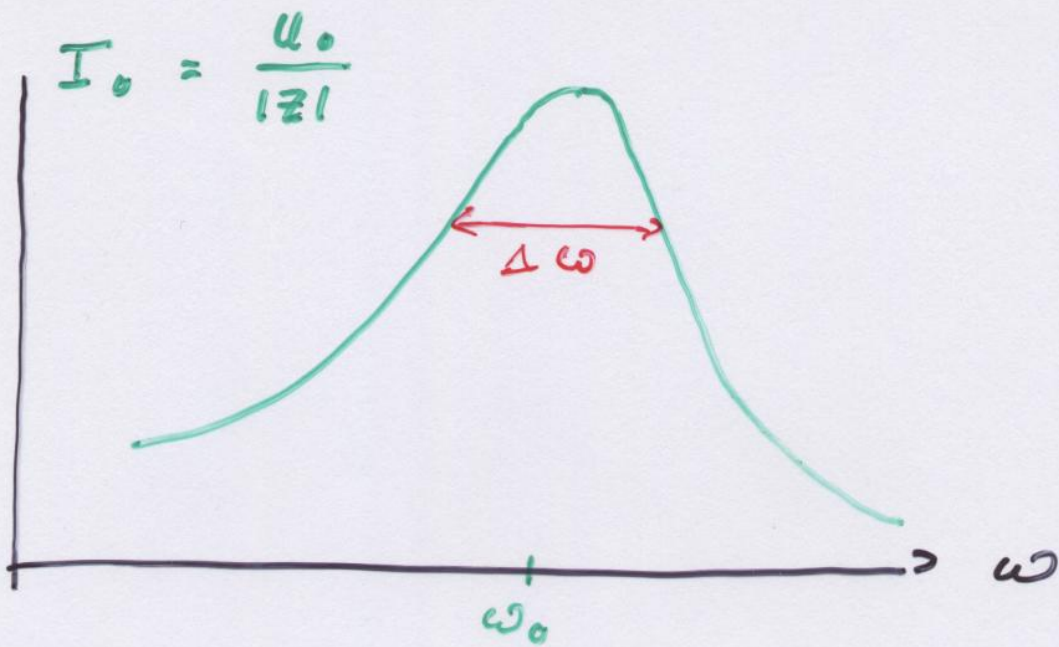
$$R_L = \sqrt{R^2 + (\omega L)^2}$$

7. Reihenkreis mit R, L, C



$$\frac{du}{dt} = R \cdot \frac{dI}{dt} + L \frac{d^2 I}{dt^2} + \frac{I}{C}$$

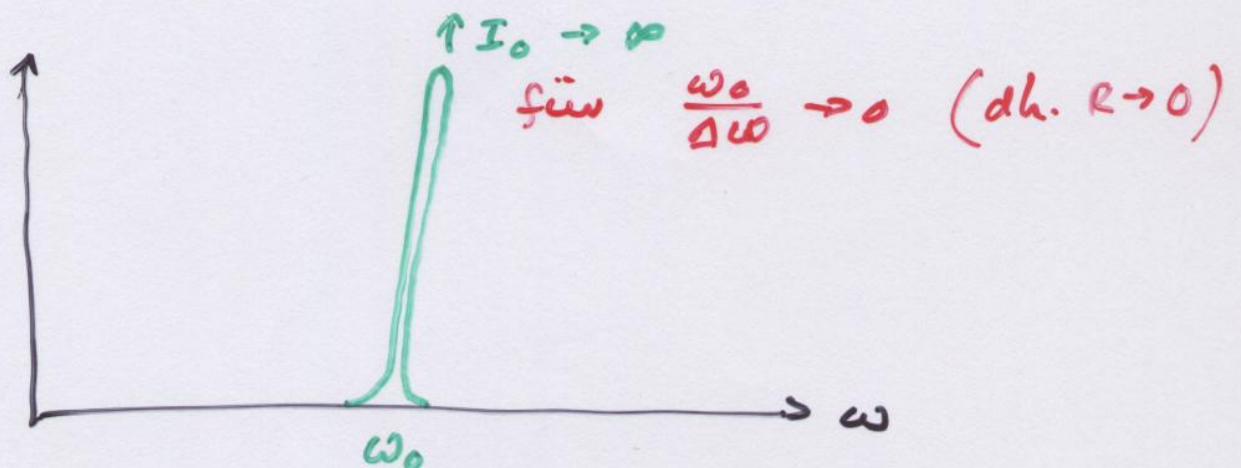
$$\text{Impedanz: } \frac{u_0}{I_0} = |Z| = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$



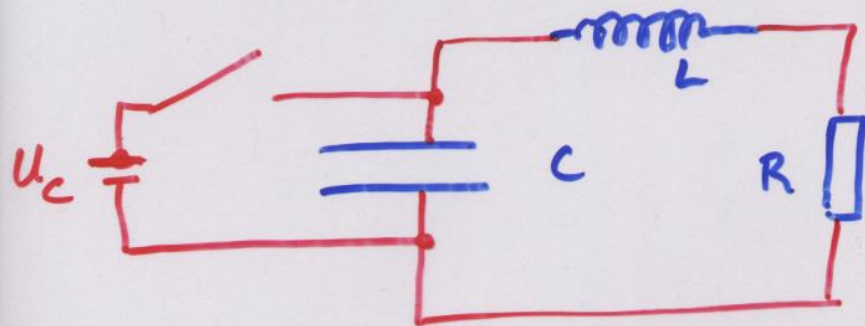
Strommaximum bei $\omega_0 L = \frac{1}{\omega_0 C}$

$$\stackrel{!}{=} \omega_0 = \frac{1}{\sqrt{LC}} \quad \text{Resonanzfrequenz}$$

Kreisgüte: $Q = \frac{\omega_0}{\Delta\omega}$



8. Serienerschwingkreis

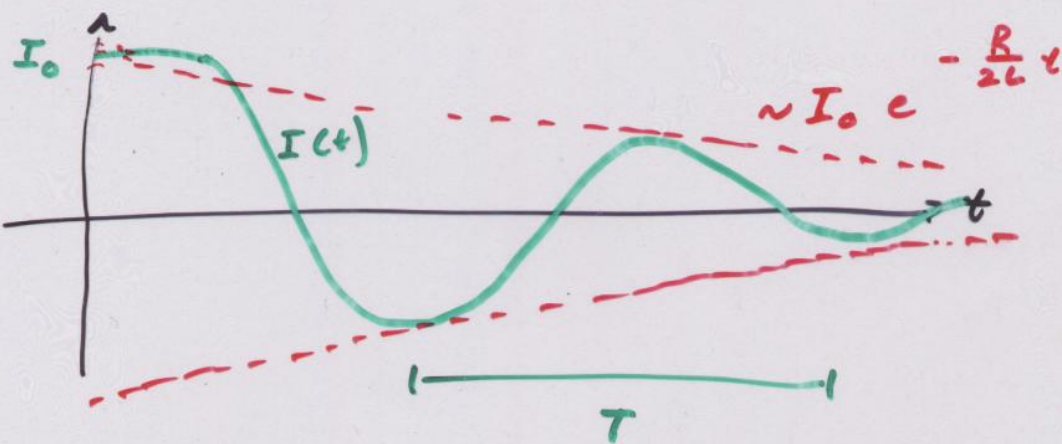


$$U_c + U_R + U_L = 0$$

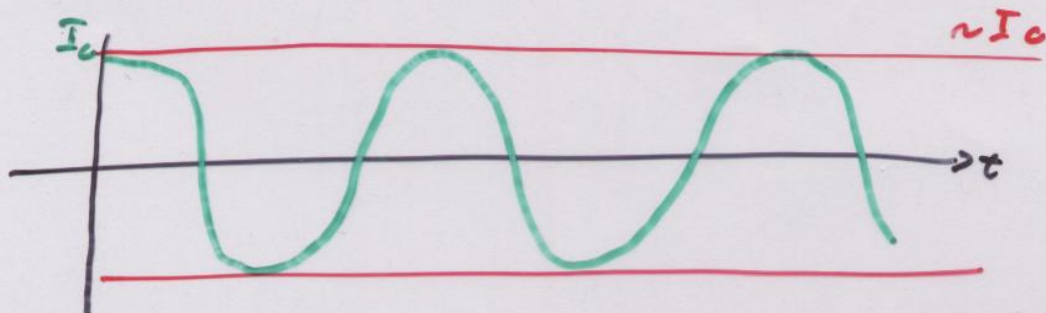
$$\Rightarrow \frac{Q}{C} + R \cdot I + L \cdot \dot{I} = 0$$

$$I(t) = I_0 \cdot e^{-\frac{R}{2L}t} \cdot \cos \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}} t$$

Bem.: U_L
nicht definiert,
siehe Einschub

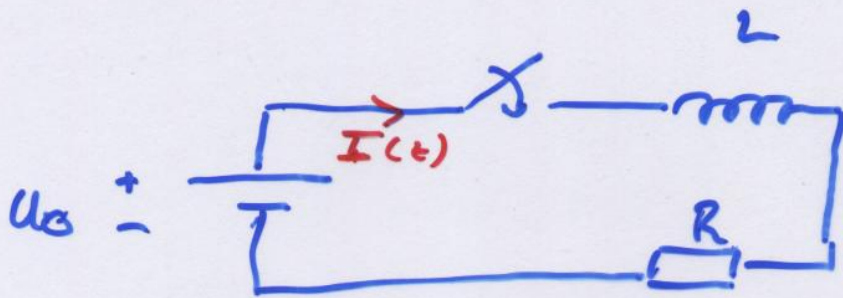


Sonderfall: $R \rightarrow 0$:



Einschub

Schaltkreis mit induktiven Komponenten

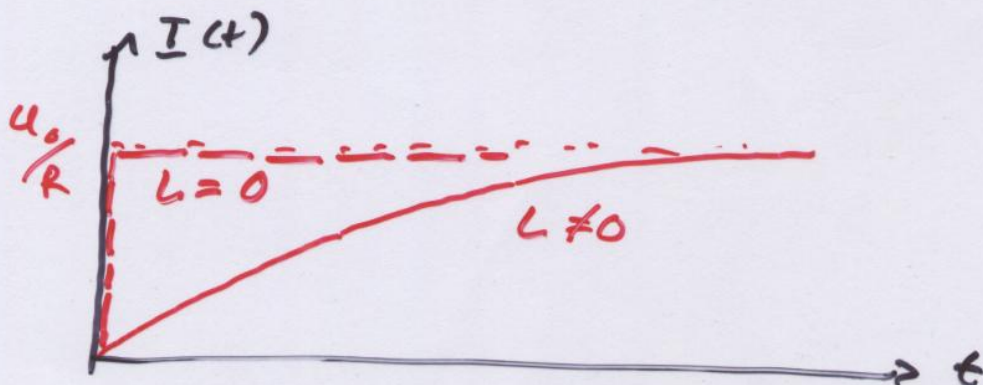


Kirchhoff: $\sum u_i = 0$ ($\oint \vec{E}(\vec{r}) d\vec{s} = 0$)
Gilt nicht für Schaltkreise mit $L \neq 0$

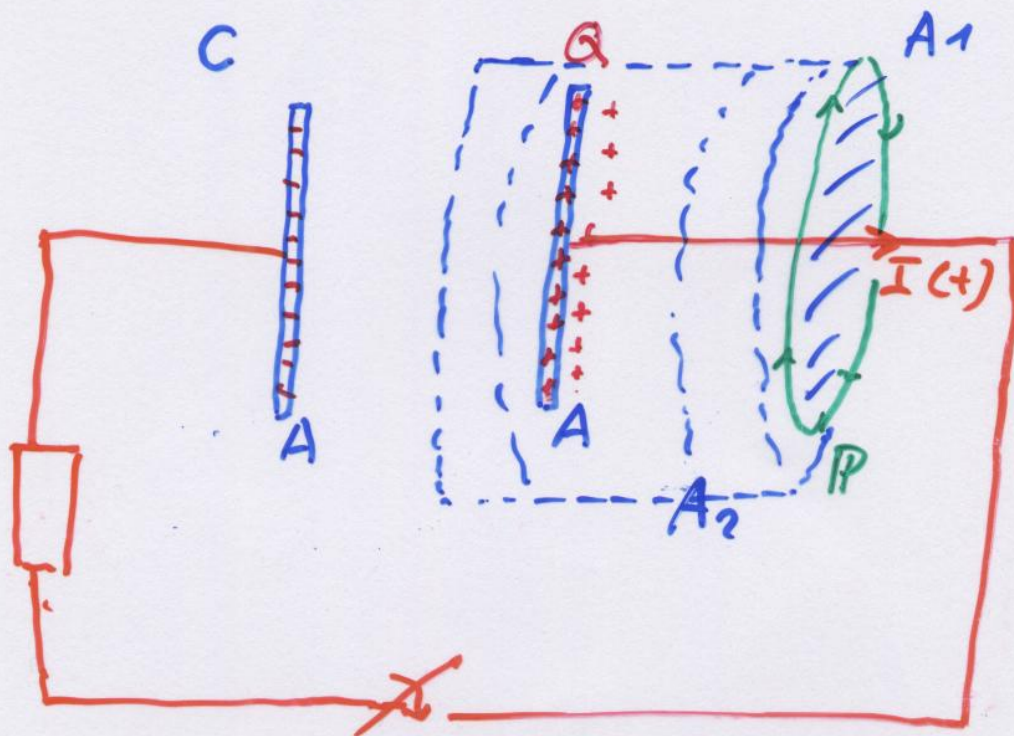
Faraday: $\oint \vec{E} d\vec{s} = - \frac{d\Phi_B}{dt}$

$$u_0 - R \cdot I(t) - L \frac{dI}{dt} = 0$$

$$\Rightarrow I(t) = \frac{u_0}{R} \cdot (1 - e^{-R/L t})$$



5.3 Maxwell'sches Verschiebungsstrom



Ampere'sches Gesetz:

$$\int_{\mathcal{P}} \vec{B} \cdot d\vec{s} = \mu_0 \cdot I$$

$$\stackrel{!}{=} \int_{A_1} \nabla \times \vec{B} \cdot d\vec{A} = \mu_0 \int_{A_1} \vec{j} \cdot d\vec{A} \quad (\text{Stokes})$$

Fläche: $A_1: \mu_0 \int_{A_1} \vec{j} \cdot d\vec{A} = I$

$A_2: \mu_0 \int_{A_2} \vec{j} \cdot d\vec{A} = 0$

↓

Zwischen den Kondensatorplatten:

zeitl. veränderliches \vec{E} -Feld

$$\frac{dQ}{dt} = \frac{d}{dt} (\epsilon_0 \cdot \vec{A} \cdot \vec{E}) = \epsilon_0 \cdot \vec{A} \cdot \frac{\partial \vec{E}}{\partial t}$$

$(Q = C \cdot U = C \cdot E \cdot d) \quad (\vec{E} = \vec{E}(x, t))$

$$= \vec{I}_v$$

$$\vec{I}_v = \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

$$\Rightarrow \int_R \vec{B} \cdot d\vec{s} = \mu_0 \int_A (\vec{j} + \vec{I}_v) \cdot d\vec{A}$$

$$\Rightarrow \nabla \times \vec{B} = \mu_0 \vec{j} + \frac{1}{c^2} \frac{\partial \vec{E}}{\partial t}$$

Betrachten Divergenzen der Gesamtstromdichte:

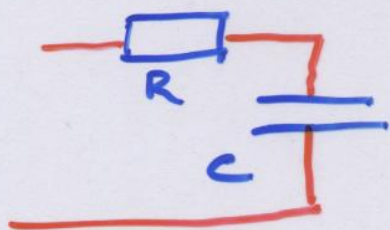
$$\mu_0 \nabla \cdot \vec{j} + \mu_0 \epsilon_0 \frac{\partial}{\partial t} \nabla \cdot \vec{E} = 0$$

$$(\nabla \cdot (\text{rot } \vec{B}) = 0)$$

$$\text{Kontinuitätsgleichung: } \nabla \cdot \vec{j} + \frac{\partial \rho}{\partial t} = 0$$

5.4. Energie des elektrischen und des magnetischen Feldes

Erinnerung:



Aufladung von C

$$\begin{aligned}dW &= dQ \cdot U \\ &= dQ \cdot \frac{Q}{C}\end{aligned}$$

$$\begin{aligned}W &= \frac{1}{C} \int Q \, dQ \\ &= \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} C U^2\end{aligned}$$

Beispiel Plattenkondensator:

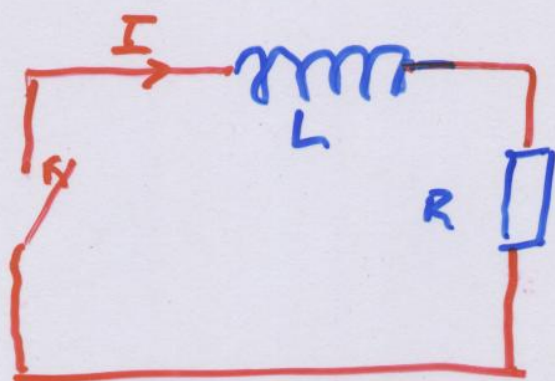
$$\begin{aligned}W &= \frac{1}{2} \frac{\epsilon_0 A}{d} \cdot E^2 d^2 \\ &= \frac{1}{2} \epsilon_0 E^2 \cdot \mathcal{V}\end{aligned}$$

Volumen

Energiedichte

$$w = \frac{W}{\mathcal{V}} = \frac{1}{2} \epsilon_0 E^2$$

Analog für Magnetfelder.

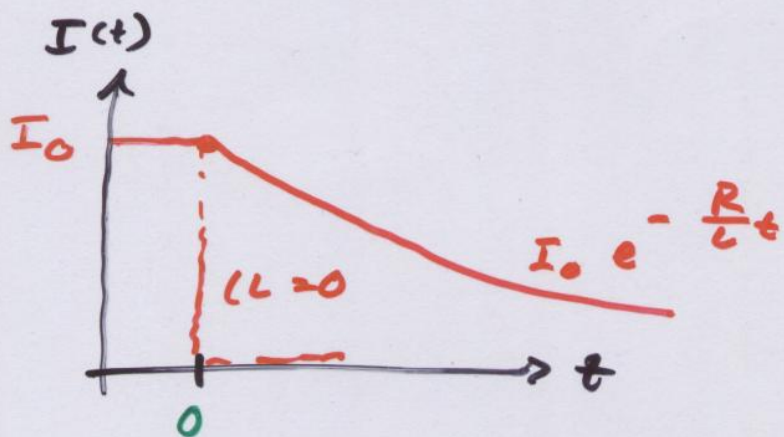


$$W = \int_0^{\infty} I U dt$$

$$= \int_0^{\infty} I^2 R dt$$

$$= \int_0^{\infty} R \cdot I_0^2 e^{-\frac{2R}{L}t} dt$$

$$= \frac{1}{2} L I_0^2$$



$$\begin{aligned} \text{Spule: } W &= \frac{1}{2} \mu_0 n^2 A l \cdot \left(\frac{B}{\mu_0 n} \right)^2 \\ &= \frac{1}{2\mu_0} B^2 \cdot V \end{aligned}$$

$$\Rightarrow \text{Energiedichte: } w = \frac{1}{2\mu_0} B^2$$